

# 國立中央大學103學年度碩士班考試入學試題卷

所別：水文與海洋科學研究所碩士班 不分組(一般生) 科目：微積分 共 1 頁 第 1 頁  
水文與海洋科學研究所碩士班 不分組(在職生)

本科考試禁用計算器

\*請在試卷答案卷(卡)內作答

1. Find the following derivatives,

(a) [10%] Given  $y = x \cos(x)$ , find  $\frac{dy}{dx}$

(b) [10%] Given  $\sin(x+y) = x$ , find  $\frac{dy}{dx}$

(c) [10%] Given  $x^2 + y^2 - 2xy = 0$ , find  $\frac{d^2y}{dx^2}$

2. [10%] Find the maximum and minimum values of the function

$$f(x) = x^3 + 3x^2 - 24x + 10, \quad -5 \leq x \leq 3$$

3. Evaluate the following integrations:

(a) [10%]  $\int \frac{1}{1+x} dx$

(b) [10%]  $\int_0^\pi e^x \sin(2x) dx$

4. Given two vectors,  $\mathbf{U} = 2\mathbf{i} + 1\mathbf{j} + 2\mathbf{k}$ , and  $\mathbf{V} = 3\mathbf{i} + 4\mathbf{j} + 2\mathbf{k}$ , find

(a) [5%] dot product of  $\mathbf{U} \cdot \mathbf{V}$

(b) [5%] cross product of  $\mathbf{U} \times \mathbf{V}$

(c) [10%] the angle between  $\mathbf{U}$  and  $\mathbf{V}$

(d) [10%] the area of triangle formed by  $\mathbf{U}$  and  $\mathbf{V}$

5. [10%] Find the Maclaurin series of  $e^x$  to four terms. (Maclaurin series is a Taylor series expansion of a function about 0)

參考用